

Recall  $u$ -substitution technique:

Last Time:

$$\int \sqrt{1+x^2} x dx$$

versus

$$\int \sqrt{1+x} x dx$$

Do:  $\int e^{5x} dx$

Do:  $\int \sin 9x dx$

Naturally,  $u$ -sub does not work in every situation.

**Recall: Derivative Product Rule**

$$[f \cdot g]' = f' \cdot g + f \cdot g'$$

then

**Another Tool: Integration by Parts (IBP)**

one function will become \_\_\_\_\_

and the other function will be \_\_\_\_\_, label it \_\_\_\_\_

ex.  $\int xe^x dx$

**IBP Formula:**

$$\int u dv = uv - \int v du$$

ex.  $\int xe^{3x} dx$

ex.  $\int x \sin x \, dx$

$$\int u \, dv = uv - \int v \, du$$

Going forward, the challenge will be to decide \_\_\_\_\_.

Do:  $\int x \sin x^2 \, dx$

Do:  $\int x \sin(2x) \, dx$

**Needing to Use IBP More Than Once:**

ex.  $\int t^2 e^t dt$

**When power function isn't  $u$ :**

ex.  $\int x^5 \ln x dx$